Sites of Rupture in Human Atherosclerotic Carotid Plaques Are Associated With High Structural Stresses
An In Vivo MRI-Based 3D Fluid-Structure Interaction Study
Dalin Tang, PhD; Zhongzhao Teng, PhD; Gador Canton, PhD; Chun Yang, MS; Marina Ferguson, BS; Xueying Huang, PhD; Jie Zheng, PhD; Pamela K. Woodard, MD; Chun Yuan, PhD

Background and Purpose—It has been hypothesized that high structural stress in atherosclerotic plaques at critical sites may contribute to plaque disruption. To test that hypothesis, 3D fluid-structure interaction models were constructed based on in vivo MRI data of human atherosclerotic carotid plaques to assess structural stress behaviors of plaques with and without rupture.

Methods—In vivo MRI data of carotid plaques from 12 patients scheduled for endarterectomy were acquired for model reconstruction. Histology confirmed that 5 of the 12 plaques had rupture. Plaque wall stress (PWS) and flow maximum shear stress were extracted from all nodal points on the lumen surface of each plaque for analysis. A critical PWS (maximum of PWS values from all possible vulnerable sites) was determined for each plaque.

Results—Mean PWS from all ulcer nodes in ruptured plaques was 86% higher than that from all nonulcer nodes (123.0 versus 66.3 kPa, \(P<0.0001\)). Mean flow maximum shear stress from all ulcer nodes in ruptured plaques was 170% higher than that from all nonulcer nodes (38.9 versus 14.4 dyn/cm², \(P<0.0001\)). Mean critical PWS from the 5 ruptured plaques was 126% higher than that from the 7 nonruptured ones (247.3 versus 108 kPa, \(P=0.0016\) using log transformation).

Conclusion—The results of this study show that plaques with prior ruptures are associated with higher critical stress conditions, both at ulcer sites and when compared with nonruptured plaques. With further validations, plaque stress analysis may provide additional stress indicators helpful for image-based plaque vulnerability assessment. (Stroke. 2009;40:3258-3263.)

Key Words: carotid artery ■ atherosclerosis ■ MRI ■ plaque rupture ■ fluid structure interaction

Atherosclerotic plaque vulnerability assessment and the ability to predict possible future plaque rupture are of vital importance for early diagnosis, prevention, and treatment of cardiovascular disease. It has been hypothesized that critical stress conditions (maximum principal stress values at critical sites where rupture is likely to occur) in the plaque may be closely related to plaque rupture and can be combined with current image-based assessment techniques for more accurate plaque evaluation and vulnerability assessment.1–2 A major challenge for all available plaque assessment schemes is the lack of realistic lesion information based on in vivo patient data where both ruptured and nonruptured plaques are compared and analyzed. In vivo patient image data showing rupture verified by histological information provided by excised specimens could help to establish an in vivo benchmark for image-based or stress-based assessment schemes.

Currently, screening and diagnosis of patients with atherosclerotic plaques is based on medical images such as magnetic resonance image (MRI), ultrasound, intravascular ultrasound (IVUS), and computerized tomography (CT). In particular, MRI techniques have been shown to be able to noninvasively characterize plaque morphology and composition, and in particular, to identify fibrous cap rupture.3–12 Chu et al performed serial high-spatial resolution, multisequence MRI studies identifying fibrous cap rupture, and a penetrating ulcer into carotid atherosclerotic plaque.10

In addition to plaque morphology, mechanical forces, considered to be potential rupture triggers, and plaque composition are key factors in the rupture process and should be considered in an integrated way for plaque assessment.12 It has been hypothesized that image-based computational fluid-structure interaction (FSI) models with accurate stress and flow information may have potential to improve the current histology- and image-based plaque assessment schemes.1–2 MRI-based computational simulations for plaque rupture investigation and vulnerability assessment have been conducted by several groups with interesting and significant results reported.13–26 Steinman et al investigated effects of

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plaque geometric features on flow behaviors using realistic plaque geometries. Holzapfel et al introduced multi-layer anisotropic plaque models and showed that stress predictions from their models could be different from single-layer isotropic models by 50% to 200% or more. Lee et al and Loree et al studied effects of plaque cap thickness and material properties on stress level and plaque rupture. Vengrenyuk and Weinbaum et al demonstrated that plaque cap with microcalcification inclusions are associated with elevated stress levels and may be related to plaque rupture. Influence of curvature dynamics and cyclic bending on coronary plaque stress and flow behaviors was investigated by Prosi et al and Tang et al. Li et al performed structure analysis based on in vivo MRI of carotid arteries and found that wall stress was higher in symptomatic patients than in asymptomatic patients. Groen and Wentzel et al in a case report indicated that plaque rupture in the carotid artery was localized at the high shear stress region. In the introduction of image-based FSI models, Tang et al demonstrated that fluid-structure interactions, axial stretch, cyclic bending, and a preshrink process for in vivo imaged-based models have considerable effects on accuracy of stress/strain predictions.

To date, evidence from 3D FSI models based on in vivo MRI data of ruptured human atherosclerotic carotid plaques linking plaque rupture to corresponding stress and flow shear stress conditions is still lacking in the current literature because of the difficulties in obtaining in vivo MRI data with indication of plaque ruptures and constructing 3D FSI models. In this study, 3D computational multi-component models with FSI were constructed based on in vivo MRI data of carotid plaques acquired from 12 patients with advanced lesions. Disruption of the plaque surface considered in this article was defined as the presence of ulcerated regions in the MR images. We evaluated plaque wall maximum principal stress (PWS) and flow maximum shear stress (FMSS) values on all lumen surface nodal points to study the associations between mechanical stress and flow shear stress conditions and plaque rupture sites.

Methods

MRI Data Acquisition

In vivo MR images of human atherosclerotic carotid plaques from 12 patients scheduled for carotid endarterectomy (age: 54 to 82, mean = 68, 11M, 1F; 5 plaques with ulcerations which are indication of prior ruptures, 7 plaques without prior rupture) were acquired before the surgery at the University of Washington, Seattle (n = 11) and Washington University, St. Louis (n = 1), and after informed consent. The institutional review boards of each institution approved the consent forms and study protocols. Patients were imaged with a 1.5-T MR scanner (Signa Horizon EchoSpeed, General Electric Health Care). Precontrast MR images included double-inversion-recovery T1-, proton density-, and T2-weighted (T1W, PDW, and T2W, respectively), and time-of-flight (TOF). Postcontrast double-inversion recovery T1W MR images of carotid arteries were obtained with a previously published standardized protocol (T1W: repetition time/echo time/inversion time, 800/10/650 ms; PDW and T2W: repetition time/echo time, 3RR, 20/40 ms; TOF: repetition time/echo time, 25/3.8 ms). A gadolinium-based contrast agent (Omniscan, Amersham Health), 0.1 mmol/kg (0.2 mL/kg) body weight, was injected intravenously with a power injector, and acquisition of postcontrast T1W images occurred 6 to 10 minutes after injection. All images were obtained with the following parameters: 16 cm field-of-view, 256 × 256 matrix size, and 2-mm slice thickness. After interpolation, the in-plane resolution is 0.31 × 0.31 mm². The longitudinal coverage covered the bulk region of each carotid lesion.

MR images were segmented using custom made analysis tools (CASCADE developed at the Vascular Imaging Laboratory at University of Washington, and APIA, from Washington University) to identify lipid-rich necrotic core, loose matrix, calcification, thrombus, hemorrhage, and the presence or absence of ulcer, as the indicator of disruption. Disruption was confirmed by the histology after matching to the MR images. The histology-validated MRI analysis of the status of the fibrous cap resulted in 5 arteries with ulcerated plaques. Figure 1 shows a plaque slice with TOF, T1-, and PD-weighted MR and histological images showing an ulcer. Figure 2 gives a set of 10 slices of PD-weighted MR images and segmented contour plots showing 3D reconstruction process.

3D Reconstruction, Shrink-Stretch Process, and Mesh Generation Process

Under the in vivo condition, the artery is axially stretched and pressurized. Disruption and circumferential shrinking was applied to generate the start-shape for the computational simulation. Shrinkage in the axial direction was 9% so that the vessel would regain its in vivo length with a 10% axial stretch. Circumferential shrinkage for lumen and outer wall was determined so that: (1) total mass volume was conserved; (2) plaque geometry after 10% axial stretch and pressurization had the best match with the original in vivo geometry. Because advanced plaques have complex irregular geometries with component inclusions that are challenging for mesh generation, a component-fitting mesh generation technique was developed to generate mesh for these models. Using this technique, the 3D plaque domain was divided into hundreds of small “volumes” to curve-fit the irregular plaque geometry with plaque component inclusions. Ulcers were replaced with lipid cores covered by a thin cap. This is our best approximation for the premature geometry of these plaque samples. 3D surfaces, volumes, and computational mesh were created with ADINA (ADINA R&D, Inc) computing environment. Each plaque model required about 3600 small volumes to be created to fit the shape of wall and adjacent components, and about 1000 small volumes were needed for the corresponding fluid domain.

FSI Computational Model

Both the artery wall and plaque components were assumed to be hyperelastic, isotropic, incompressible, and homogeneous. Blood flow was assumed to be laminar, Newtonian, viscous, and incompressible. The incompressible Navier-Stokes equations with arbitrary Lagrangian-Eulerian (ALE) formulation were used as the governing
equations. A no-slip condition between all interfaces was assumed. Patient-specific systolic and diastolic pressure conditions from the last hospital admission were used to impose pulsatile pressure conditions at the inlet and outlet of the artery. The modified Mooney-Rivlin model was used to describe the material property of each component in the plaque.\textsuperscript{25–26,28}

\begin{equation}
W = c_1 \{I_1 \} - 3 + c_2 \{I_2 \} - 3 + D_1 \left[ \exp \left( D_2 \{I_1 \} - 3 \right) - 1 \right].
\end{equation}

where \(I_1\) is the first strain invariant, \(C = \{C_{ij}\}\) is the right Cauchy-Green deformation tensor, \(X = [X_{ij} \} = \{\partial x_i / \partial a_j\} \), \(x_i\) is current position, \(a_i\) is original position, \(c_1\) and \(D_1\) are material parameters chosen to match experimental measurement.\textsuperscript{25–26} In this article, the following parameter values were chosen: vessel/fibrous cap, \(c_1 = 36.8\) KPa, \(D_1 = 1.44\) KPa, \(D_2 = 2\); calcification, \(c_1 = 368\) KPa, \(D_1 = 144\) KPa, \(D_2 = 2.0\); lipid core/hemorrhage/ulcers, \(c_1 = 2\) KPa, \(D_1 = 2\) KPa, \(D_2 = 1.5\); loose matrix, \(c_1 = 18.4\) KPa, \(D_1 = 7.2\) kPa, \(D_2 = 1.5\). \(c_2 = 0\) was set for all materials.

Solution Method

The coupled FSI plaque models were solved by a commercial finite-element package ADINA. This software uses unstructured finite element methods for both fluid and solid models. Nonlinear incremental iterative procedures were used to handle fluid-structure interactions. The governing finite element equations for both the solid and fluid models were solved by the Newton-Raphson iteration method. Details of the models and methods are given in Tang et al.\textsuperscript{25–26} and Bathe.\textsuperscript{28}

Plaque Stress/Strain and Flow Shear Stress

Data Extraction

Data for PWS and FMSS were extracted from 3D FSI solutions for all integral nodes (total nodes: structure = 7028; fluid = 6418) on lumen surfaces of 12 plaque models for analysis. Each node was assigned a node type (lipid, calcification, ulcer, loose matrix, and wall) if the node was not covering any component) according to its location and nearby component. Mean values of PWS, PWSN, and FMSS for each node type from each patient were calculated for analysis and comparisons. A t-test (\(P < 0.05\)) was used to determine whether there was a significant difference between the data compared.

Using previously published critical site selection method and critical stress approach,\textsuperscript{2} a critical PWS (CPWS) is determined for each plaque. CPWS was defined as the maximum of PWS values from all possible vulnerable sites which included sites with local stress concentration (local maximum), especially where a thin cap was covering a plaque component, but excluded healthy sites where rupture is unlikely, even if a local stress maximum occurred there.

Results

Figure 3 gives an overview of solution features from 3D FSI models using the plaque sample given in Figure 2. Maximum principal stress (Stress-P\(_1\)) on stacked cross-section slices, a bifurcation cut (B-cut) surface, and a cross-section cut (at S7 location) were plotted showing the site of rupture. Maximum Stress-P\(_1\) was observed at the site of rupture. To analyze mechanical conditions (structural stress and flow shear stress) on the lumen surface corresponding to different tissue types and to identify differences between ulcer and nonulcer nodes, data were extracted from the full 3D FSI solutions and mean values of PWS and FMSS of ulcer, lipid core, calcification, wall, and all nonulcer nodes are summarized in Tables 1 and 2. kPa and dyn/cm\(^2\) were used as the units for PWS and FMSS, respectively (1 kPa = 10\(^4\) dyn/cm\(^2\)).

Ulcer Nodes Are Associated With Higher PWS Values Compared to Nonulcer Nodes

For the 5 plaques with ulcers, the mean PWS value from all ulcer nodes was 123.0 kPa, which is 86% higher than the mean PWS value (66.3 kPa) from all nonulcer nodes (\(P < 0.0001\)). The differences between the individual mean PWS values from ulcer and nonulcer nodes for each of the 5 plaque samples were also statistically significant. Excluding the ulcer nodes, the differences between the mean PWS values from lipid, wall, and all nonulcer nodes are modest (<5%).

Overall Results Showing Ulcer Nodes Are Associated With Higher FMSS

Table 2 indicates that mean FMSS from all ulcer nodes (38.9 dyn/cm\(^2\)) was 170% higher than that (14.4 dyn/cm\(^2\)) from all nonulcer nodes for the 5 plaques with ulcerations. Individual plaque mean FMSS data showed mixed results. Three plaques...
showed mean FMSS values on ulcer nodes were greater than those on nonulcer nodes (23.6, 49.0, 54.7) versus (16.2, 9.90, 7.13), \( P < 0.0001 \); one plaque showed mean FMSS (10.8) on ulcer nodes was less than mean FMSS (18.0) on nonulcer nodes (\( P = 0.0001 \)); another plaque showed mean FMSS (39.3) was greater than that (34.1) on nonulcer nodes, but the difference was not statistically significant (\( P = 0.6848 \)).

Comparison of Plaques With Ruptures (\( n = 5 \)) and Plaques Without Rupture (\( n = 7 \))

Tables 1 and 2 list mean values of PWS and FMSS of the 2 groups of plaques on different node types; all nodes combined; and all nonulcer nodes combined. Excluding the ulcer nodes, differences of those mean values between the ruptured and nonruptured groups are not significant.

Critical Stress Values From Plaques With Rupture Were Significantly Higher Than Those from Nonruptured Plaques

CPWS values from the 5 plaques with rupture were (unit: kPa): 457.85, 241.90, 195.51, 161.92, and 179.14 with an average \( 247.3 \pm 121.4 \). CPWS values from the 7 nonruptured plaques were: 81.68, 129.31, 103.68, 143.70, 94.32, 102.88, and 108.03 with average \( 109.1 \pm 21.0 \). The average CPWS from the

<table>
<thead>
<tr>
<th>Case</th>
<th>Ulcer</th>
<th>Wall</th>
<th>Lipid</th>
<th>Calcification</th>
<th>All Nodes</th>
<th>All Nonulcer</th>
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<tr>
<td></td>
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</table>

\( n \) indicates number of nodes.

The \( P \) values are for the ulcer vs nonulcer comparisons. Unit for PWS: kPa.
5 ruptured cases was 126% higher than that from the 7 nonruptured cases (P < 0.0016 using log transformation).

**Discussion**

**In Vivo Evidence Linking Localized Stress Conditions to Plaque Vulnerability**

This is the first study with a relative large in vivo patient data in a mechanical analysis. The results showed evidence that high plaque stresses are indeed linked to sites of plaque rupture. The lesions studied were all advanced complex plaques, 5 of them having an ulcerated surface. Evidence linking local critical stress conditions with actual plaque rupture sites based on in vivo data are of great importance in establishing the benchmark for atherosclerotic plaque mechanical assessment.2

**The Role of Flow Shear Stress in Plaque Rupture Process**

Numerous studies have attempted to determine a solid link between flow shear stress and plaque progression and rupture. Groen and Wentzel et al reported a follow-up case study showing high flow shear stress region was associated with site of plaque rupture.24 The overall results from this study are supporting their findings. Individual differences suggest that larger-scale study is needed to further clarify the role of FMSS in the rupture process. Considering that critical structural stress is at about 100 to 400 kPa level and FMSS is only at <10 Pa, contribution from flow shear stress acting as a rupture trigger may be much smaller than that from structural stress. However, high flow shear stress may act on the lumen surface in a long-term process leading to endothelial dysfunction and lumen surface weakening.

**Limitations**

The models used in the study made use of patient-specific plaque morphology and systolic/diastolic pressure conditions with the intent for potential patient-screening applications. However, the models lack patient-specific vessel and plaque component material properties because of an inability to measure these material properties in vivo using the current imaging format. Accurate anisotropic vessel and plaque component material property measurements will improve the model predictions. The accuracy of the computational models when compared to histology is also compromised by the limited in vivo MRI resolution (0.31 × 0.31 × 2.0 mm³).

It is known that blood flow in carotid arteries with severe stenosis may become disturbed or even turbulent.29 Although many flow and geometric parameters may affect flow behavior, considerable turbulence can be present when stenosis severity (based on the diameter measurement) exceeds 70%.29 Stenosis severity (based on diameter) of the 12 plaques was <40% in 7 cases, <55% in 4 cases, <75% in one case. Although the choice of laminar flow model may be justified for this study, as only one case exceeded the stenosis degree that guarantees turbulent Reynolds number, a turbulent model will be considered in future studies for better predictions. Local disturbed flow behaviors were complex and may be reported in future studies.

**Conclusion**

The results from 3D FSI models based on in vivo MRI data for human carotid plaques (5 with ruptures, 7 nonruptures) show that plaques with prior ruptures are associated with higher critical plaque wall stress conditions when compared with nonruptured plaques and that those high critical stress conditions occur at ulcer sites. These findings, when further validated in a
larger study, may provide additional stress indicators helpful for image-based plaque vulnerability assessment.

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**Disclosures**

None.

**References**


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